Abstention from smoking extends life and compresses morbidity: a population based study of health expectancy among smokers and never smokers in Denmark

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Abstract
Objective—To estimate health expectancy—that is, the average lifetime in good health—among never smokers, ex-smokers, and smokers in Denmark.

Design—A method suggested by Peto and colleagues in 1992 for estimating smoking attributable mortality rates was used to construct a life table for never smokers. This life table and relative risks for death for ex-smokers and smokers versus never smokers were used to estimate life tables for ex-smokers and smokers. Life tables and prevalence rates of health status were combined and health expectancy was calculated by Sullivan’s method.

Setting—The Danish adult population.

Main outcome measures—The expected lifetime in self rated good health or without longstanding illness for never smokers and smokers.

Results—The expected lifetime of a 20 year old man who will never begin to smoke is 56.7 years, 48.7 (95% confidence interval (CI) 46.8 to 50.7) years of which are expected to be in self rated good health. The corresponding figures for a man who smokes heavily are 49.5 years, 36.5 (95% CI 35.0 to 38.1) years of which are in self rated good health. A 20 year old woman who will never begin to smoke can expect to live a further 60.9 years, with 46.4 (95% CI 44.9 to 47.8) years in self rated good health; if she is a lifelong heavy smoker, her expected lifetime is reduced to 53.8 years, 33.8 (95% CI 31.7 to 35.9) years of which are in self rated good health. Health expectancy based on long standing illness is reduced for smokers when compared with never smokers.

Conclusions—Smoking reduces the expected lifetime in good health and increases the expected lifetime in poor health.

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Keywords: life expectancy; health expectancy

The health risks of tobacco smoking are well known. If nobody in Denmark died because of smoking, life expectancy would increase by about three years for men and two years for women.1 Smoking increases the risks for lung and other cancers, diseases of the respiratory system, diseases of the circulatory system, and other diseases. Smoking attributable deaths in Denmark in 1995 accounted for 25% of all deaths among men and 18% among women.1 The impact of tobacco smoking on public health can also be evaluated by comparing health expectancy—that is, the average lifetime in good health—between never smokers and smokers; furthermore, the hypothesis that abstention from smoking compresses morbidity can be examined.2

To our knowledge, the effect of smoking on health expectancy has not previously been estimated from national data. The purpose of the present study was to compare expected lifetime in self rated good health or without longstanding illness between Danish never smokers and smokers.

Methods
A commonly used method for health expectancy calculation is Sullivan’s method.3 The method requires life tables and data on the prevalence of health status. Thus, to estimate health expectancy among never smokers, ex-smokers, moderate, and heavy smokers we need life tables for each smoking category. The first step in the calculation of health expectancy is therefore to construct these life tables. The Danish National Cohort Study (DANCOS), established by linking data from the Danish Health Interview Survey for 1987, 1991, and 1994 with the Cause of Death Register and other national registers does not include enough persons followed up for a sufficient length of time to estimate life tables classified by sex and smoking category. But DANCOS makes it possible to estimate relative risks for death for ex-, moderate, and heavy smokers versus never smokers. The relative risk estimates and a life table for never smokers constructed on the basis of a method proposed by Peto and colleagues4 can be used to estimate life tables classified by sex and smoking category. The final step in estimating health expectancy is to combine life table data and prevalence of health status by smoking category. The details of the calculations are described below.

ESTIMATING LIFE TABLES FOR NEVER SMOKERS, EX-SMOKERS, AND SMOKERS
The sizes of the second prospective Cancer Prevention Study (CPS-II) of the American Cancer Society on smoking and mortality allowed estimation of lung cancer death rates among people who had never smoked. By use of a method suggested by Peto and colleagues,5 we calculated the proportion of smoking...
attributable deaths from lung cancer in 1991 to 1995 from the rates of death from lung cancer in Denmark and the rates for never smokers and smokers estimated from the CPS-II. We then estimated a sex and age specific “synthetic smoking prevalence” rate for Denmark, which is the prevalence that would be necessary to result in the observed rate of death from lung cancer in the population. Indirectly it includes the influence of the proportion of smokers, the amount smoked, the duration of smoking, the age at starting to smoke, and the prevalence of inhaling. On the basis of the “synthetic smoking prevalence” and relative risks taken from the CPS-II, we calculated the aetiological fractions for other smoking related causes of death: upper aerodigestive cancers, other cancers, chronic obstructive lung disease, other diseases of the respiratory system, vascular diseases, and other natural causes. However, in order to control for confounding and ensure that the hazards of tobacco were not exaggerated the aetiological fraction \( P(RR-1) / (1+P(RR-1)) \) was replaced by \( P(RR-1) / (2+P(RR-1)) \), according to the method of Peto and colleagues. Thus, deaths caused by smoking and deaths not caused by smoking were calculated. In particular, life tables for never smoking men and women could be estimated. DANCOS made it possible to estimate relative risks for death for ex-, moderate, and heavy smokers versus never smokers. The estimates found were 1.1 for ex-smokers, 1.3 for moderate smokers, and 2.2 for heavy smokers. Age specific death rates for never smokers were multiplied by relative risk estimates giving age specific death rates for each smoking category. Nevertheless, because of the long delay before smoker’s risk for death is increased, the relative risks (RRs) for people under 45 were reduced to \( (RR+1)/2 \). Finally, life tables by smoking category were constructed. The method is described in greater detail in appendix 1.

**Danish Health Interview Survey Data**

Data on the health of the Danish population were collected in 1991 and 1994 by interviewing representative, random samples of Danes extracted from the Danish Civil Registration System. Each of the two independent cross sectional surveys comprised approximately 6000 Danes aged 16 years or over. In order to eliminate seasonal variation, interviews were conducted in three rounds, in February, May, and September, each comprising about 2000 interviews, by professional interviewers from the Danish National Institute of Social Research who were carefully instructed before visiting the participants. In the 1991 survey, questions on smoking were asked only in the third round, and only data from that round were included in the present study. Interviews were obtained with about 80% of the subjects. The rate of refusal to participate was almost the same for men and women, but it increased with age and was highest among single persons and among persons in the metropolitan area.

As the questions in the two health surveys that were relevant for this study were identical, the data were combined and were considered to represent the health status of Danish adult at the beginning of the 1990s. The present study included respondents aged 20 years or more, comprising 2766 men and 3045 women.

Self rated health was based on answers to the question: “How would you rate your present state of health in general?” The five original response categories (very good, good, fair, poor, and very poor) were dichotomised into “good” and “fair or poor”. Longstanding illness was determined on the basis of answers to the question: “Do you suffer from any longstanding illness, longstanding sequelae from injury, handicap or other longstanding complaint?” Whenever longstanding illness was reported, its nature was clarified by means of an open question. The answers to this question were subsequently coded according to the World Health Organization’s International Classification of Diseases and grouped into one of 14 disease groups.

The interviewees were categorised as never smokers, ex-smokers, moderate smokers (1-14 g of tobacco per day), and heavy smokers (≥ 15 g of tobacco per day) according to answers to the question “Do you smoke?” with the answer categories “Yes, daily”, “Yes, but some days I don’t smoke”, and “No”, and questions on the amount of tobacco smoked. The question: “Have you ever been a smoker?” was asked to identify ex-smokers.

**Estimating Health Expectancy**

Health expectancy was calculated by Sullivan’s method, by combining life tables and prevalence rates of health status. On the basis of the life table figures, we calculated the expected numbers of years lived in age groups of five years. The proportion of healthy people in each age group was taken from the health survey data, and the number of years in good health was estimated. Health expectancy from a given age was then calculated by adding these years and relating the sum to the number of survivors at that age. By relating health expectancy to life expectancy, a measure of the proportion of lifetime in good health was established. Confidence intervals were estimated by the formulae suggested by the International Network on Health Expectancy (REVEs). The method is summarised in appendix 2.

**Results**

Life expectancy at age 20 was seven years shorter for heavy smokers than for never smokers, whereas, at age 65, the difference was a little more than five years. Life expectancy for a never smoking 20 year old man was 56.7 years, 48.7 of which were expected to be spent in self rated good health. The expected lifetime in self rated fair or poor health was 8.0 years (56.7 years − 48.7 years). The 48.7 years in good health account for 85.9% of the remaining expected lifetime of 56.7 years (table 1). A 20 year old male lifelong heavy smoker could expect to live only 36.5 years of his remaining lifetime of 49.5 years in self rated good health.
Table 1  Expected lifetime and proportion of expected lifetime in self rated good health at ages 20 and 65 among never smokers, ex-smokers, moderate smokers, and heavy smokers

<table>
<thead>
<tr>
<th>Age</th>
<th>Smoking category</th>
<th>Life expectancy (years)</th>
<th>Expected lifetime in self rated good health (years (95% CI))</th>
<th>Proportion of expected good health (% (95% CI))</th>
<th>Reduced life expectancy (years)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Men</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>Never smoker</td>
<td>56.7</td>
<td>48.3 (34.2 to 39.0)</td>
<td>64.5 (60.3 to 68.7)</td>
<td>5.2 (3.4 to 7.0)</td>
</tr>
<tr>
<td></td>
<td>Ex-smoker</td>
<td>55.9</td>
<td>39.5 (32.9 to 37.0)</td>
<td>62.6 (58.9 to 66.2)</td>
<td>5.0 (4.2 to 5.8)</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>54.3</td>
<td>36.0 (33.8 to 38.2)</td>
<td>66.3 (62.0 to 70.4)</td>
<td>4.6 (3.7 to 5.4)</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>49.5</td>
<td>29.0 (27.2 to 30.7)</td>
<td>58.5 (55.0 to 62.0)</td>
<td>4.5 (3.5 to 5.5)</td>
</tr>
<tr>
<td></td>
<td>All</td>
<td>53.7</td>
<td>33.5 (32.4 to 34.5)</td>
<td>62.5 (60.5 to 64.3)</td>
<td>5.2 (4.3 to 6.1)</td>
</tr>
<tr>
<td>65</td>
<td>Never smoker</td>
<td>16.4</td>
<td>11.7 (9.8 to 13.6)</td>
<td>71.2 (59.8 to 82.6)</td>
<td>4.6 (3.8 to 5.4)</td>
</tr>
<tr>
<td></td>
<td>Ex-smoker</td>
<td>15.7</td>
<td>9.3 (8.3 to 10.3)</td>
<td>59.1 (52.7 to 65.6)</td>
<td>5.0 (4.2 to 5.8)</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>14.6</td>
<td>9.3 (8.0 to 10.7)</td>
<td>61.4 (54.9 to 73.3)</td>
<td>5.1 (4.3 to 5.9)</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>11.2</td>
<td>6.9 (5.9 to 7.9)</td>
<td>61.6 (52.7 to 71.0)</td>
<td>5.3 (4.4 to 6.2)</td>
</tr>
<tr>
<td></td>
<td>All</td>
<td>14.2</td>
<td>8.8 (8.2 to 9.4)</td>
<td>62.0 (57.7 to 66.3)</td>
<td>5.4 (4.6 to 6.3)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Women</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>Never smoker</td>
<td>5.4</td>
<td>4.7 (4.1 to 5.3)</td>
<td>72.6 (63.8 to 81.4)</td>
<td>0.7 (0.5 to 0.9)</td>
</tr>
<tr>
<td></td>
<td>Ex-smoker</td>
<td>7.3</td>
<td>4.8 (4.3 to 5.3)</td>
<td>73.5 (64.7 to 82.3)</td>
<td>1.0 (0.8 to 1.2)</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>9.3</td>
<td>6.6 (5.9 to 7.4)</td>
<td>71.1 (62.5 to 79.7)</td>
<td>1.6 (1.4 to 1.8)</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>11.2</td>
<td>6.9 (5.9 to 7.9)</td>
<td>61.6 (52.7 to 71.0)</td>
<td>2.0 (1.6 to 2.4)</td>
</tr>
<tr>
<td></td>
<td>All</td>
<td>14.2</td>
<td>8.8 (8.2 to 9.4)</td>
<td>62.0 (57.7 to 66.3)</td>
<td>2.1 (1.8 to 2.4)</td>
</tr>
<tr>
<td>65</td>
<td>Never smoker</td>
<td>7.2</td>
<td>6.5 (6.0 to 7.0)</td>
<td>71.8 (63.1 to 80.5)</td>
<td>1.2 (1.0 to 1.4)</td>
</tr>
<tr>
<td></td>
<td>Ex-smoker</td>
<td>9.1</td>
<td>6.9 (6.4 to 7.4)</td>
<td>71.1 (62.5 to 79.7)</td>
<td>1.6 (1.4 to 1.8)</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>11.0</td>
<td>7.7 (7.2 to 8.2)</td>
<td>71.1 (62.5 to 79.7)</td>
<td>2.0 (1.6 to 2.4)</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>12.5</td>
<td>8.1 (7.6 to 8.6)</td>
<td>61.6 (52.7 to 71.0)</td>
<td>2.5 (2.1 to 2.8)</td>
</tr>
<tr>
<td></td>
<td>All</td>
<td>15.0</td>
<td>8.8 (8.3 to 9.3)</td>
<td>62.0 (57.7 to 66.3)</td>
<td>2.8 (2.4 to 3.1)</td>
</tr>
</tbody>
</table>

And 13.0 years in fair or poor health. The corresponding results for ex-smokers and moderate smokers lay between those of never smokers and heavy smokers (table 1). Analogous differences were found for 20 year old never smoking, ex-smoking, and smoking women (table 1), and a similar pattern was seen at older ages. The results for 65 year olds are shown in table 1.

Table 2 shows that the expected lifetime without longstanding illness for a 20 year old male lifelong heavy smoker was 29.0 years, which was 7.6 years shorter than that of a never smoking man. The expected lifetime with longstanding illness of 20 year old men was about 20 years for both never smokers and heavy smokers. For women, the situation was even worse, the difference in expected lifetime without longstanding illness being 11.4 years. A 20 year old female lifelong heavy smoker could expect 4.3 years more with longstanding illness than a never smoker. No significant difference in expected lifetime without longstanding illness was found between never smokers, ex-smokers, and moderate smokers.

The columns in tables 1 and 2 showing the proportion of expected lifetime in self rated good health and without longstanding illness, respectively, show the compression of morbidity achieved by abstention from smoking. This is further elucidated in absolute terms in table 3, showing the difference in the numbers of expected healthy and unhealthy life-years between never smokers and ex-, moderate, and heavy smokers. For instance, a 20 year old male lifelong heavy smoker could expect to lose 12.2 years in self rated good health and add 5.0 years in fair or poor health.

Musculoskeletal diseases accounted for the highest proportion of longstanding illness, and could expect 4.6 years more with longstanding illness than a never smoker. No significant difference in expected lifetime without longstanding illness was found between never smokers, ex-smokers, and moderate smokers.

Table 3 Reduction in life expectancy, expected healthy life-years lost and expected unhealthy life-years added for 20 and 65 year old ex-, moderate, and heavy smokers compared with never smokers

<table>
<thead>
<tr>
<th>Age</th>
<th>Smoking category</th>
<th>Sex</th>
<th>Reduced life expectancy (years)</th>
<th>Expected healthy life-years lost</th>
<th>Expected unhealthy life-years added</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Men</td>
<td></td>
<td>In self rated good health (%)</td>
<td>Without longstanding illness (%)</td>
</tr>
<tr>
<td>20</td>
<td>Ex-smoker</td>
<td>0.9</td>
<td>3.7</td>
<td>1.6</td>
<td>0.8</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>0.9</td>
<td>3.9</td>
<td>1.6</td>
<td>0.8</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>0.9</td>
<td>3.9</td>
<td>1.6</td>
<td>0.8</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Women</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>Ex-smoker</td>
<td>0.7</td>
<td>2.4</td>
<td>1.3</td>
<td>1.1</td>
</tr>
<tr>
<td></td>
<td>Moderate smoker</td>
<td>0.7</td>
<td>2.4</td>
<td>1.3</td>
<td>1.1</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>0.7</td>
<td>2.4</td>
<td>1.3</td>
<td>1.1</td>
</tr>
<tr>
<td>65</td>
<td>Ex-smoker</td>
<td>0.7</td>
<td>2.4</td>
<td>1.3</td>
<td>1.1</td>
</tr>
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<td></td>
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<td>0.7</td>
<td>2.4</td>
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<td>1.1</td>
</tr>
<tr>
<td></td>
<td>Heavy smoker</td>
<td>0.7</td>
<td>2.4</td>
<td>1.3</td>
<td>1.1</td>
</tr>
</tbody>
</table>
heavy smokers could expect at least as many years with musculoskeletal diseases as never smokers, ex-, and moderate smokers (data not shown). Twenty year old men who will never begin to smoke, ex-smokers, moderate, and heavy smokers could expect 1.7 years, 3.5 years, 3.0 years, and 2.7 years encumbered with diseases of the respiratory system, respectively. The corresponding figures for 20 year old women were 2.0 years, 3.3 years, 3.0 years, and 5.2 years.

SENSITIVITY ANALYSIS
The results rely among other things on the relative risk estimates from DANCOS. To test how sensitive the results were to changes in relative risks, we estimated life tables and expected lifetime without longstanding illness using the upper limits of the 95% confidence intervals of the relative risk estimates, which were 1.3 for ex-smokers, 1.5 for moderate smokers, and 2.7 for heavy smokers. One result of this choice of relative risks was a less agreement between death rates aggregated over smoking category and the combined death rates of never smokers, ex-smokers, moderate smokers, and heavy smokers (that is, the right hand values of the equation \( R = P \cdot R_1 + P \cdot R_2 + P \cdot R_3 + P \cdot R_4 \), which was used to control the calculations, were generally too high, appendix 1). The life expectancy of 20 year old lifelong heavy smokers was reduced to 47.7 years for men and 51.9 years for women—that is, nine years lower than that of never smokers. The expected lifetime without longstanding illness was reduced by 0.7 years for male heavy smokers and 0.2 years for women, and the conclusions were not significantly affected by this change of relative risks.

Although individuals with poor health might be more likely not to participate in interview surveys about health, a difference in participation rates by smoking habit is implausible. Because the health of smokers is poorer than that of non-smokers, however, the differences in health expectancy might be slightly underestimated. Thus, if the proportion of persons suffering from longstanding illness were increased by 5%, the difference in the expected lifetime without longstanding illness between 20 year old never smokers and lifelong heavy smokers would increase by 0.1 years.

Discussion
The main questions with regard to the validity of the results are whether:
- life tables for never smokers are reliable—that is, whether the estimate of smoking related mortality can be trusted;
- life tables for ex-smokers and smokers are reliable—that is, whether the DANCOS estimates of relative risks can be trusted;
- reports of smoking habits and self rated health and longstanding illness in the health interview surveys are reliable.

The first question addresses the validity of the method of Peto and colleagues’ for estimating smoking related mortality. The method was evaluated in two recent studies, both including mortality rates in Denmark, and the results were found to be reasonable.\(^9\) Thus, the numbers of smoking attributable deaths from lung cancer, chronic bronchitis, emphysema, ischemic heart disease, and stroke were estimated by the method of Peto and by the simulation model “Prevent”, and close agreement between the two methods was found.\(^9\) The Prevent model\(^10\) takes into account the development of smoking habits for a period of 20 years, whereas the Peto method does not require information about smoking, because the estimated synthetic smoking prevalence summarises the history of smoking in the population.

Two aspects must be considered in answering the second question: (1) the age and sex specific death rates in the various smoking categories must be consistent with the crude age and sex specific death rates—generally, we found the demand for consistency satisfactorily fulfilled; (2) when the relative risk estimates from DANCOS were replaced by the upper limits of the confidence intervals, as described in the section on sensitivity analysis, the gap between the life expectancy of never smokers and smokers was widened but did not change the conclusion as to differences in expected lifetime without longstanding illness between never smokers, ex-smokers, and smokers. Furthermore, the DANCOS estimates are fairly close to similar estimates from other studies including Danish data.\(^7\)\(^11\)

Self reported data on smoking habits tend to result in an underestimate of smoking prevalence.\(^12\) This misclassification could lead to an underestimate of the difference in health expectancy between smoking categories. Another possible bias might be introduced by the non-response rate of 20%—for example, if the responders were healthier than the non-responders. The assumption that the prevalence of longstanding illness was in fact 5% higher did not alter the conclusion as to differences between smoking categories. The reliability of measures of self rated health has been investigated in several studies. Thus, the test-retest reliability of self rated health was found to be good or even better than that of more specific questions in two Swedish surveys.\(^13\) In a Danish study comprising three surveys it was concluded that self rated health is an independent concept.\(^14\) Moreover, a review of literature showed that self rated health is a powerful predictor of mortality and other health related end points.\(^15\) Thus, the answer to the third question is that the obvious weaknesses in health interview survey data will not invalidate the results.

The proportion of expected lifetime in self rated good health (table 1) or without longstanding illness (table 2) is shorter for women than for men. This is a general result and not specifically Danish. Differences between the sexes and between socioeconomic groups in health expectancy have been reported earlier.\(^16\)\(^17\)

We conclude that the estimates of health expectancy estimates are reliable and can withstand minor changes, reflecting the uncertainty
Smoking abstention extends life

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The results of these studies generally indicate that 6–9 life-years are lost because of smoking. Another key statistic is the mean years lost per death from smoking which was estimated at 13 years and 14 years for Danish men and women, respectively. The results from the various studies depend on the population (national or subpopulations, such as the British doctors) and the method of calculation—for example, whether ex-smokers are included in the group of non-smokers or whether smokers are divided into light, moderate, and heavy smokers. To our knowledge, only two studies of the extent of loss of life-years in good and in poor health have been published. A recent study on the relation between smoking, physical activity, and active life expectancy in a US population aged ≥ 65 years showed that disability-free life expectancy was longest for never smokers who were physically active and shortest for inactive ever smokers. A Dutch study showed that abstention from smoking extends life and increases the length of time without disability.

Appendix 1: construction of life tables for never smokers, ex-smokers, moderate smokers, and heavy smokers on the basis of the method of Peto and colleagues.

Let L signify the sex and age specific Danish lung cancer death rate and A and C the lung cancer death rates among never smokers and smokers, respectively, according to the CPS-II. The “synthetic smoking prevalence” is then:

\[ P = \frac{(L - 0)}{(C - 0)} \]

Let RR signify the CPS-II estimate of the relative risk for a smoking related disease other than lung cancer. Then, the aetiological fraction is:

\[ \frac{P(RR - 1)}{1 + P(RR - 1)} \]

In order to ensure that the hazards of tobacco are not exaggerated, the conservative estimate is used:

This method can be used to estimate sex and age specific mortality rates caused by smoking. Thus, sex and age specific death rates, \( R_0 \), and a life table for never smokers can be estimated.

Appendix 2: calculation of health expectancy by the method of Sullivan

Let \( l(x) \) and \( e(x) \) signify the conventional life table figures of survivors and life expectancy at age \( x \). If \( p(x,x+n) \) is the prevalence of good health at age \( x \) to \( x+n \) among \( N(x,x+n) \) responders, then the expected years of life in good health among the \( l(x) \) survivors at age \( x \) to \( x+n \) is:

\[ H(x,x+n) = \frac{1}{N(x,x+n)} \sum_{x-x+n} l(x)e(x) - l(x+n)e(x+n) \times p(x,x+n) \]

The health expectancy of a \( x \) year old person is:

\[ HLE(x_0) = \frac{1}{l(x_0)} \sum_{x-x_0} H(x_0,x+n) \]

The variance of \( HLE(x_0) \) is approximated by:

\[ \text{Var}(HLE(x_0)) = \frac{1}{l(x_0)} \sum_{x-x_0} \left[ \frac{(x)e(x) - l(x+n)e(x+n))^2 \times p(x,x+n) \times (1 - p(x,x+n))}{N(x,x+n)} \right] \]


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